

Whitell (T) and Dauncible (J) H 5-a-b

By the KING's Patent.

A

530. i. 35.
5

T R E A T I S E
UPON THE
DENDROMETER,

A

New-invented INSTRUMENT

F O R

The more certain and ready Measurement of
Standing Timber, BY INSPECTION ONLY:

F O R

Facilitating the practical Operations of Engineering,
Land-surveying, Levelling, Mineing, &c.

AND FOR

Performing mechanically the various Cases of Plane
Trigonometry, by a short and familiar Process,
WITHOUT CALCULATION.



L O N D O N,

Printed for the PATENTEES:

And sold by F. NEWBERY, in Ludgate-Street; J. BENNETT,
Instrument-maker to their Royal Highnesses the Duke of
GLOCESTER and Duke of CUMBERLAND, in Crown-Court,
Soho; B. COLE, Instrument-maker, in Fleet-Street; and
T. WHITELL, in Pater-noster-Row.

By whom SUBSCRIPTIONS are received.

П. Г. А. Ф. Я. Т.
С. А. Ф. Я. Т.
Я. Т. М. Я. Д. И. Е.

Т. Я. Д. И. Е. К.

З. Я. Д. И. Е. К.

Я. Т. М. Я. Д. И. Е.

Д. И. Е. К.



Д. И. Е. К.

Д. И. Е. К.

TO THE
RIGHT HONOURABLE
THE
EARL OF MORTON,
&c. &c. &c.

President of the Royal Society, &c.

THIS
T R E A T I S E
UPON THE
D E N D R O M E T E R

Is most humbly inscribed,

By His LORDSHIP's much obliged,

and most devoted humble Servants,

Thomas Whittell,
John Duncombe.

ант от

ПРЕДСЕДАТЕЛЯ ТОГОИ

ант

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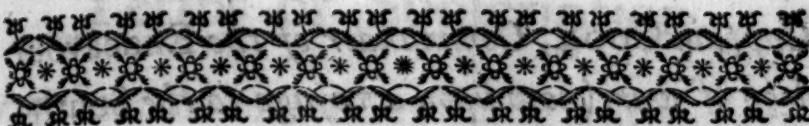
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P R E F A C E.

BEFORE we enter upon the subject of the following sheets, we cannot sufficiently express the grateful sense we entertain of His MAJESTY's condescension, in being graciously pleased to permit us to exemplify the utility of our Instrument in HIS ROYAL PRESENCE.

We are highly obliged to the Right Honourable the Earl of MORTON, and the rest of the members of the ROYAL SOCIETY, for the very candid and favourable reception, which the invention met with from that illustrious body.

Our particular acknowledgments are due to the learned J. BEVIS, M. D. Mr. COWLEY, Professor of Mathematics at the Royal Academy at Woolwich; Mr. SAMUEL CLARK, Teacher of the Mathematics in London; to

Captain

P R E F A C E.

Captain Cook, Commander of the Endeavour sloop of war (now upon a voyage to the South-Seas to observe the transit of Venus) and to sundry other ingenious Gentlemen; by whose kind assistance we have been enabled to make divers improvements both in the Book and Instrument.

We should with pleasure acknowledge the many personal civilities, which, in the course of our application, we have experienced from several of the Nobility and Gentry—especially from two Noble Lords, and one Gentleman of distinguished eminence in point of abilities and merit:—But as we are not at liberty to mention their names, we must leave them to the highest gratification of benevolent minds, the satisfaction resulting from acts of goodness and generosity.



Terms

Terms of Subscription.

THE DENDROMETER (to be delivered with all possible expedition) completely finished under the care of the INVENTOR, assisted by Dr. BEVIS, &c. fitted to a proper theodolite, and contrived to act either separately therefrom, or jointly therewith, with elegant mahogany-case, &c. - - - - Twenty-five Guineas.

To Gentlemen already possessed of a theodolite, the DENDROMETER, completely made and fitted thereto, - - - - Ten Guineas.

The DENDROMETER alone, to act without a theodolite, for the use of measuring standing trees, with proper staff, case, &c.

Fifteen Guineas.

The expence of procuring the King's Patent, the making of the Instruments, and other incidents, being much greater than was, at first, apprehended—the Patentees are induced to hope that the Subscribers will have no objection to deposite Five Guineas in part of payment, upon receiving a receipt under the hands of persons, properly authorized, that the same shall be allowed upon delivery of the Instrument.

That Messrs. F. NEWBERY, J. BENNETT, B. COLE, and T. WHITTELL, are properly authorized by the Patentees to receive the said Five Guineas, and to give receipts for the same under their own hands, and NO ONE ELSE.

ADVERTISEMENT.

THE PATENTEES of the DENDROMETER take the Liberty to acquaint the Public, that His Majesty has been graciously pleased to grant them his Royal LETTERS PATENT for a JACK, upon a Construction singularly new and useful. It is so contrived, as to continue going for six Hours successively, by a small Weight, from the Height of six Feet only; and, when down, may be wound up with the greatest Ease. It will turn a Joint of Meat of any Size, and is so certain in its Execution, as to require no Attendance. It is also calculated to shew the *Time*, as a Clock, while going. It is not apt to be out of Order, nor subject to the Expence and Trouble of Lines and Pulleys; the many Difficulties of conveying them through different Rooms; the Danger of the ponderous Weight hanging to the Jacks in present Use; the frequent Necessity and vast Difficulty of winding them up; nor the continual Charges of a Smoke-Jack. The Price will be different, according to their Size and Finishing. The same, upon a more enlarged Plan, is intended to serve (instead of a Fire or other Engine) to raise Water out of Mines; whereby a prodigious Expence will be saved to the Proprietors thereof.

N. B. An Assortment will be finished with as much Expedition as possible.

Any Persons inclined to favour the PATENTEES with their Commands, are desired to write (Post paid) to Mr. Thomas Whittell, in *Pater-noster-Row, London.*

INTRODUCTION.



infiniti iacti, non solum adiutoria, sed etiam
ad integrum libri operis, etiamque

INTRODUCTION.



T is almost needless to mention, that the present method of measuring standing timber is very defective, and erroneous; notwithstanding the many attempts, which have been made, to render it easy and certain. There is *no* instrument, we apprehend, hitherto made public, which *can* give the measurement with any degree of precision. The quadrant, altho' of extensive use and application, will by no means answer that particular purpose: for, if the tree should either incline, or recline; or the ground, whence the observation is to be made, be irregular in the least, the

measurement must be vague and erroneous. To prove the truth of this assertion, we shall take the liberty to quote the following general rules, for the use of that instrument, from the learned and ingenious Doctor * Harris: *viz.* “ On the *quadrant* “ you have a line called the *quadrat*, “ which hath two sides, divided each into “ 100 equal parts; and that on the left “ hand is called *right shadow*, and that on “ the right hand *contrary shadow*. By “ which means ‘tis very easy to take any “ accessible altitude at one station by the “ *quadrant*. For, if the angle be just 45° , “ the distance to the foot of the *object* from “ the station is equal to the altitude; but “ if the angle be less than that, the “ string will fall on *right shadow* in the “ *quadrat*. Then say, as 100 is to the “ number of parts of the *right shadow*, cut “ by the string, so is the distance to the alti- “ tude. So that if the string cut 25, 75,

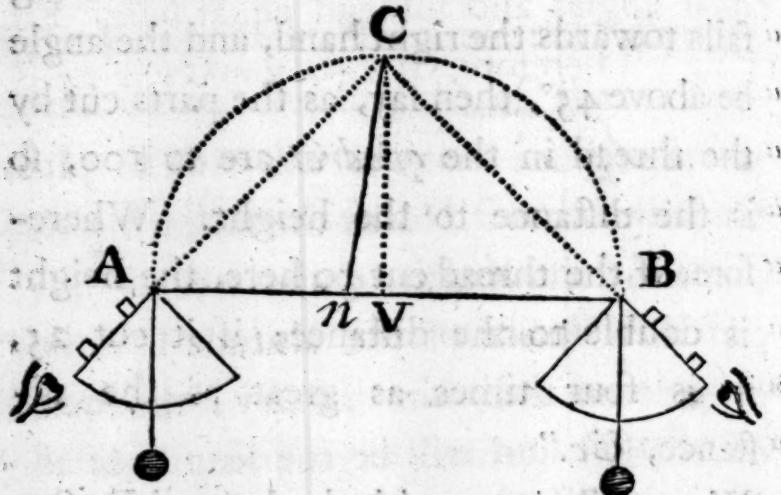
* Lexicon Technicum, Vol. I. Title *Altitudes*.

" or 50, &c. the height is accordingly $\frac{1}{4}$, $\frac{3}{4}$,
 " or $\frac{1}{2}$ the distance. But when the string
 " falls towards the right hand, and the angle
 " be above 45° , then say, as the parts cut by
 " the thread in the quadrat are to 100, so
 " is the distance to the height. Where-
 " fore, if the thread cut 50 here, the height
 " is double to the distance; if it cut 25,
 " it is four times as great as the di-
 " stance, &c."

We readily agree with the learned Doctor in this respect, provided the object be perpendicular, and the ground horizontal: for altitudes of objects are always measured by the nearest distances from their horizontal or level bases. But, on the other hand, if either the object vary from a perpendicular position, or be situated on sloping ground, there must be an error; as may be proved thus:

[4]

EXAMPLE I.



Let Cn represent a tree standing upon the horizontal base AnB , whose reclinature nv from the perpendicular Cv being given: to find the length nC .

Make an observation at A , causing the plummet to hang directly over the 45th degree; then should An be equal to Cn by the first general rule: But $Cn = An + nv + Cn - Cv$; as is evident by the above figure.

ILLUSTRATION.

Suppose $An = 20$ F. and $nv = 4$ F. then is $An + nv = 24$ F. Now, the angle at v being a right one, and the angle of observation at A being 45° , the angles ACv ,

CAv

Cv will be equal, Corol. 4. Eu. 32. i.

Equal angles also subtend equal sides, Eu.

6. i. Therefore, $An + nv = Cv = 24$ F.

Again, $\sqrt{Cv^2 + nv^2} = Cn = 24$ F. 3 I. 4,

&c. Eu. 47. i. Hence the following rule
for finding the length of the tree :

To the square of the altitude Cv , add
the square of the reclination nv ; the square
root of that sum will be the length of the
tree Cn required.

EXAMPLE II.

Other things remaining as before, let B
now be the place of observation, (the plumb-
met still cutting the 45th degree) and the
horizontal line Bv being equal to 24 F. To
find the length of the tree Cn .

Here Bn should be equal to Cn by the
first general rule: But $Cn = Bn - nv + Cv$
 $- Cv$; as by the above figure.

ILLUSTRATION.

Now Bn being equal to 28 F. and nv
 $= 4$ F. then $Bn - nv = 24$ F. The angle
at v is a right one, and the angle of obser-

vation at B is 45° ; therefore the angles $\nu C B$, $C B \nu$ are equal, Corol. 4. Eu. 32. I. Equal angles subtend equal sides, Eu. 6. I. Hence $B n - n \nu = C \nu = 24 F.$ Again,

$$\sqrt{C \nu^2 + n^2} = C n = 24 F. 3 I. \frac{3}{4}, \text{ &c.}$$

Eu. 47. I.

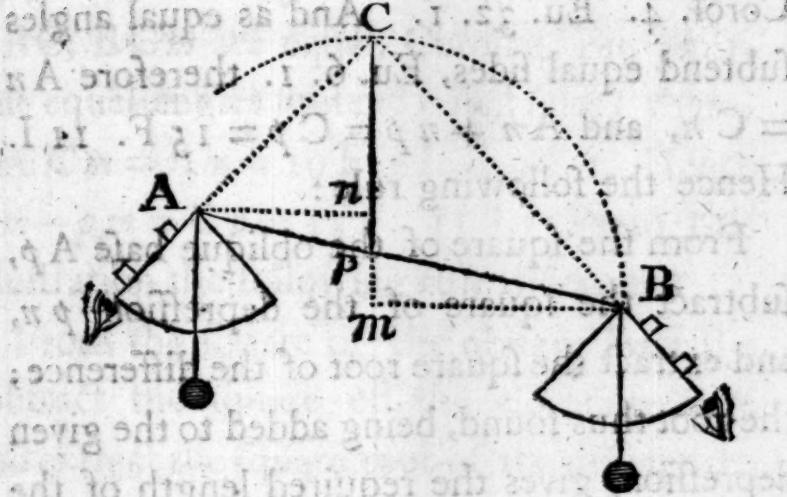
From this illustration it follows, that the square root of the sum of the squares of the altitude $C \nu$, and relevation $n \nu$, gives the length of the tree $C n$ the same as before.

Having shewn the inutility of the quadrant when applied to measuring trees, in an oblique position, standing on horizontal bases; we shall next proceed to point out such errors as will arise in the computation, when they are situated on ascending or descending planes.

EXAMPLE

EXAMPLE III. Let $j = \frac{1}{2}$

EXAMPLE III.



Let Cp represent a tree standing perpendicular to the horizontal line An , upon a descending plane ApB , whose depression pn being given; to find the length of the said tree. Make an observation at A , causing the plummet to hang directly over the 45th degree: then should Ap be equal to pC by the first general Rule: but $Cp = Ap + np$ — $\overline{Ap - An}$ by the figure.

ILLUSTRATION.

Suppose $A\dot{p}$ equal to 14 F. and the depression $n\dot{p}$ equal to 2 F. then $\sqrt{A\dot{p}^2 - n\dot{p}^2} = A\dot{n} = 13$ F. 11 I. Eu. 47. i. The angle

at n being a right one, and the angle nAC 45° , it follows, that ACn is also 45° , by Corol. 4. Eu. 32. i. And as equal angles subtend equal sides, Eu. 6. i. therefore $An = Cn$, and $An + np = Cp = 15 F. 11 I.$ Hence the following rule:

From the square of the oblique base Ap , subtract the square of the depression pn , and extract the square root of the difference; the root thus found, being added to the given depression, gives the required length of the tree.

EXAMPIE IV.

Cp representing the tree, as before, let the observation be made at B , the plummet still cutting the 45 th degree of the quadrant, then should Bp be equal to Cp , by the first general rule: but $Cp = Bp - pm - \overline{Bp} - \overline{Bm}$, by the figure.

ILLUSTRATION.

Let Bp be equal to $19 F. 5 I.$ and pm (the elevation of the ascending plane BpA above the horizontal line Bm) equal to $3 F.$

$$3 I. \text{ then } \sqrt{\overline{Bp}^2 - \overline{pm}^2} = Bm = 19 F. 2 I.$$

Eu.

Eu. 47. i. Now the angle CmB being 90° , and the angle mBC 45° , the angles mBC , BCm are equal, Corol. 4. Eu. 32. i. But equal angles subtend equal sides; therefore $Cm = Bm = 19$ F. 2 I. Eu. 6. i. Hence $Bm - pm = Cp = 15$ F. 11 I. From this illustration the following rule is derived:

From the square of the oblique base Bp subtract the square of the elevation mp , and extract the square root of the difference; from this root subtract the elevation, and the remainder is the length of the tree.

Thus having shewn the insufficiency of the quadrant, in measuring the length of trees not exactly perpendicular to the horizon, nor situated upon a level base; it seems altogether needless to add, that neither the theodolite, nor any other graduated instrument of the like nature, can give the true measurement of objects, such as these, whose forms and situation are so extremely various and uncertain.

The author of this work having had frequent occasion to observe the uncertainty of measuring standing timber, unassisted

by

by any proper instrument for that purpose, conceived his present design of rendering the practice more certain and familiar, both to the owner and surveyor. In this pursuit many difficulties have occurred : how far he has obviated them, is humbly submitted to the reader's determination.

The instrument now offered to the public, called a DENDROMETER,— for which His Majesty has been pleased to grant His Royal Letters Patent,—is an invention entirely new. It is founded upon that branch of the mathematics called plane trigonometry, and its principles are chiefly derived from the 2d, 4th, 5th, 6th, and 33d propositions of the sixth book of Euclid. It is formed to measure, with great accuracy, not only the length and diameter of any tree, in any situation, but also the length and diameter of the boughs, *by inspection only*; and thence by the help of tables (hereunto annexed) the certain quantity of timber is obtained *without calculation or the use of the sliding-rule*. By this means a criterion is fixed between the buyer and seller

seller of an article, which becomes, every day, more and more valuable; as either party will have it easily in his power to prevent error, or to detect imposition.

But, notwithstanding the measuring of standing trees with ease and certainty may be esteemed no inconsiderable acquisition; yet, we presume, that this instrument, when fitted to a theodolite, will be found applicable to more extensive and important purposes: *viz.*

For the practical measurement of the heights and distances of objects, accessible or inaccessible, whether situated in planes parallel, or oblique, to the plane in which the instrument is placed.

For the taking of all angles, whether vertical, horizontal, or oblique, in any position of the planes in which they are formed; whereby the sides and angles of all plane triangles, right-angled or oblique, are determined upon the instrument, *without any trigonometrical computations*, from the usual *data*; and that, whether level to the line of station, elevated above

or

or depressed below the same, accessible or inaccessible, upon their own planes, and also upon the plane of the horizon.

From the above circumstances, it need not be urged how useful it will be found in field-operations, particularly in the practice of engineering and land-surveying : For, by the method of applying the altimeter, elevation-index, and other moveable parts of the instrument, the measure of the required sides and angles (right or oblique) is determined to sufficient exactness *without any computation*, or the use of tables, hitherto necessary to assist the theodolite and all other graduated instruments.

In the practice of engineering, we apprehend, it will be found particularly useful; as not only the distance from any fortification, but also from any visible part or projection thereof, together with the situation of the plane and place (with respect to the fortification) whereon a battery is proper to be raised, may all be readily obtained, without being under the necessity (according to the present mode of practice) of advancing

vancing upon the spot, or of approaching too near to the fire of the enemy.

We also conceive, it will be found exceedingly useful to a field officer under the following circumstance. Suppose a body of the enemy are perceived, by the General, advancing on full speed towards his army, and no time allowed for making variety of observations: by means of this instrument he can quickly discover (by lines drawn from the points of observation to the extremities of the rear of that body) the angles made, and thence the number of soldiers contained therein, which will enable him to direct, with very little trouble, what force to march against them.

Then its usefulness in land-surveying, especially on hilly or irregular ground, we apprehend, will be evident, when our readers are informed that the perpendicular rise or fall of the land, the hypothenuse, and baseline, necessary for protraction, are determined at once upon the instrument without

out calculation, and consequently without the risk of error.

In the course of this work, some things which were omitted, and others which appeared not sufficiently clear to our judicious friends, are added by way of APPENDIX. But still, if there should remain any obscure passages, we shall with pleasure endeavour to elucidate them, at the request of any person, who will give himself the trouble of pointing them out.

We shall now proceed to give a particular description of the instrument, with plain directions for the use of it. The Tables * annexed are calculated to shew the whole quantity of timber contained in any tree, of any diameter, girth, and length, both by the exact and common method; by which means, the error in the usual way of measuring round timber, so much

* They are carried from 6 in. to 80 f. in length, and from 6 in. to 4 f. 3 in. $\frac{3}{4}$ in diameter, and are so contrived as to admit of being easily extended to any further dimensions.

to the loss of the seller*, is discovered and corrected.

To conclude, if, by this invention, the measurement of standing trees be rendered easy and *certain*, and the practical operations of engineering, surveying, levelling, mining, &c. greatly facilitated, we flatter ourselves it will meet with encouragement suitable to its merit and importance.

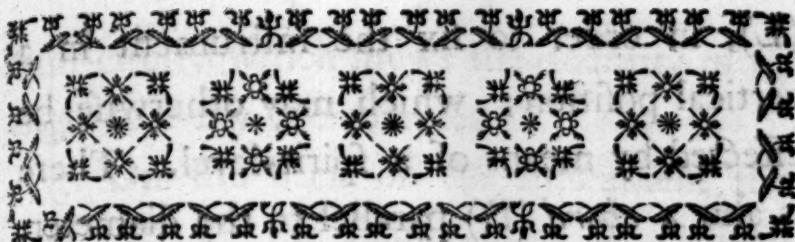
* It is obvious, that the present method of measuring timber is greatly to the disadvantage of the seller: for, by taking the girth in the middle, and $\frac{1}{4}$ of the circumference in inches for the square, the larger the tree, the greater must be the loss of the seller, even to $\frac{1}{3}$ of the contents in a tree of 48 inches circumference.



DESCRIPTION

beispielsweise die *Stellteile* oder die *Abbildung* einer *Geometrischen Figur* auf einer *Zeichenebene*. Die *Geometrische Figur* ist hierbei ein *geometrisches Objekt*, das aus *geometrischen Punkten* besteht. Ein *geometrischer Punkt* ist eine *geometrische Einheit*, die durch *geometrische Maße* wie *Länge*, *Fläche* oder *Volumen* definiert wird. Die *Abbildung* einer *Geometrischen Figur* auf einer *Zeichenebene* ist eine *geometrische Abbildung*, die die *geometrischen Punkte* der *Geometrischen Figur* in entsprechende *geometrische Punkte* auf der *Zeichenebene* überführt. Diese Abbildung kann durch verschiedene Methoden wie *geometrische Konstruktionen* oder *geometrische Transformationen* realisiert werden.

Description



DESCRIPTION OF THE DENDROMETER.

HIS instrument (which gives
a direct and general solution
of the whole *thirteen cases* in
plane trigonometry, without
calculation) is composed of divers members
or parts, *viz.*,

i. A *semi-circle* (A), which is divided
into two equal parts or quadrants. The
circumference of these quadrants are each
divided into ninety degrees, &c. beginning
at the middle of the semi-circle; and upon
the *diameter* (B) thereof hangs a *plummet*
(L),

(L), in order to fix the instrument in a vertical position; which may otherwise be effected by means of a spirit-level. There is also a *chord* (D) parallel to the diameter, and likewise a *radius* (E), which passes at right angles through the diameter and chord.

2. From a point on the radius hangs an *altimeter* (C), between the chord and diameter, to which is fixed a *small semi-circle* (G), and a screw to confine it in any position. The *altimeter*, which is contrived to form the same angle with the radius of the instrument as the tree forms with the horizon, is divided from its center both ways, each into forty equal parts; and these again, by smaller divisions, into halves and quarters. Upon the *small semi-circle* (G), on which is accounted the quantity of the angle made by the altimeter and radius, are expressed from 60 to 120 degrees, being 30 on each quadrant. The *radius* is numbered with the same scale of divisions as the altimeter. There is also a *nonius* to the small semi-

semi-circle, which shews the quantity of an angle to every five minutes.

3. On the back of the instrument the stock (M) of the sliding-piece is confined to the axis (N), which moves concentrically parallel to the elevation-index (F) on the opposite side, it being confined thereto. This index is numbered by a scale of equal divisions with the altimeter and radius. At the end thereof is a *nonius*, by which the angles of elevation above, or depression below, the horizon (measured upon the semi-circle of the instrument) are determined to every five minutes. There is also a groove in the radius, that slides across the axis by means of a screw (I), working between the chord and semi-circle of the instrument.

4. Upon the stock is a *sliding-piece* (P), that always acts at right angles with the altimeter, by means of a groove in the latter. To the shank of the sliding-piece is affixed a *moveable limb* (Q), which forms the same angle with the altimeter, as

the

the bough forms with the body, or trunk, of the tree. This *limb* may be of any convenient length, divided into equal parts of the same scale with all the foregoing divisions. At the extremity of the fixed axis, on a center, an *index* (R) with telescopic sights works horizontally upon the moveable limb of the sliding-piece.

Upon this *horizontal index* (R) may be fixed a *small quadrant* (T), (described with any convenient radius from the center whereon the index moves) divided into 90 degrees, beginning at a right line drawn from the center at right angles with the fiducial edge of the said index; and upon the extremity of the axis a *nonius*, whereby to determine the quantity of an angle upon the quadrant to every five minutes. There are also two *small circular arches* (S), serving to keep the sights in a parallel position, each containing an equal number of degrees. Upon these *arches* is measured the angle, subtending a side equal to the difference of the altitudes of the observed

observed objects above the plane of the horizon, and whose base is the nearest distance between the perpendiculars, in which the said objects are situated.

N. B. The Dendrometer is fitted to a theodolite, and may be used either separately therefrom or jointly therewith, as choice may direct, or occasion require.

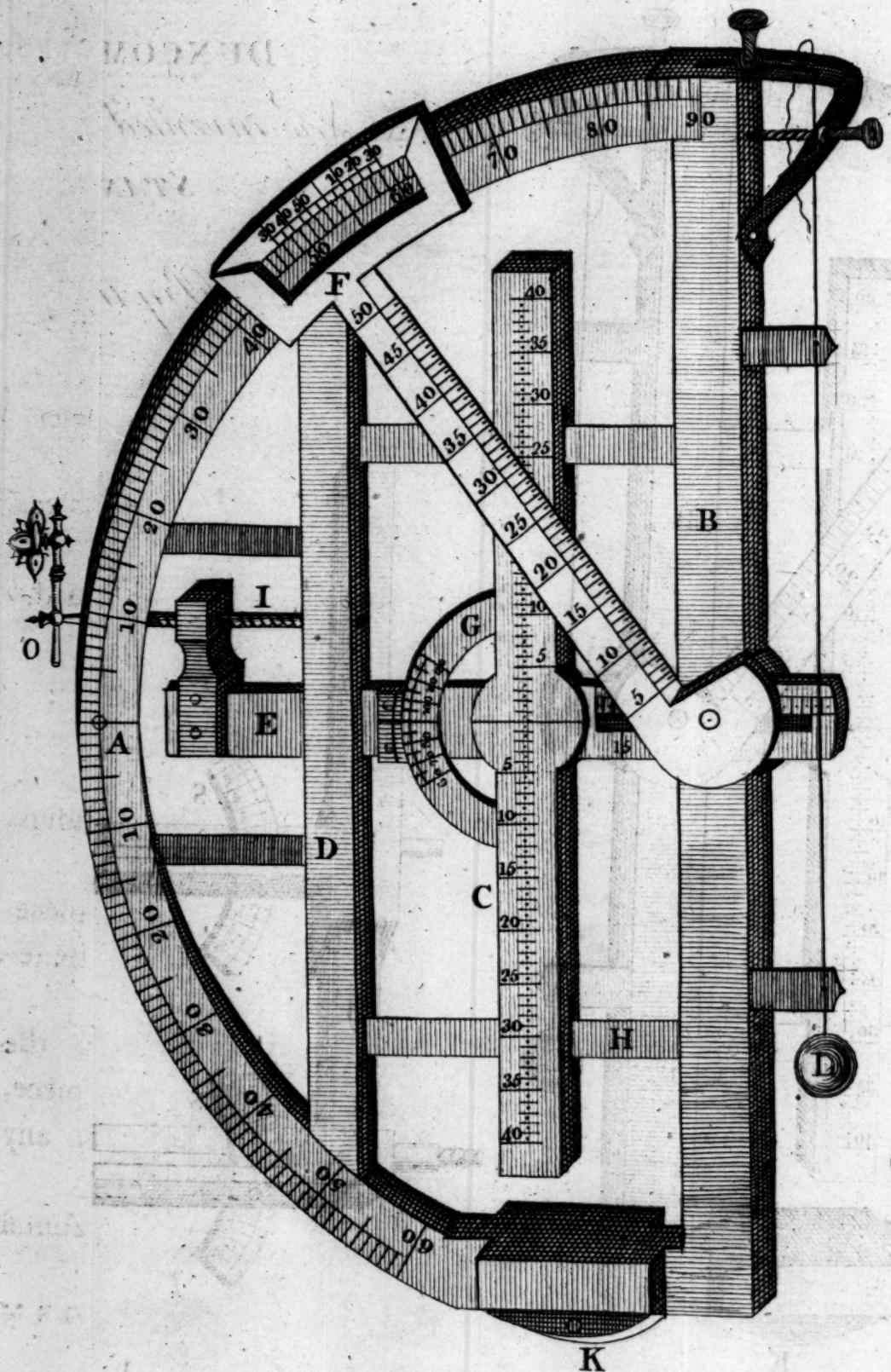


REFERENCE

REFERENCE to the PLATE.

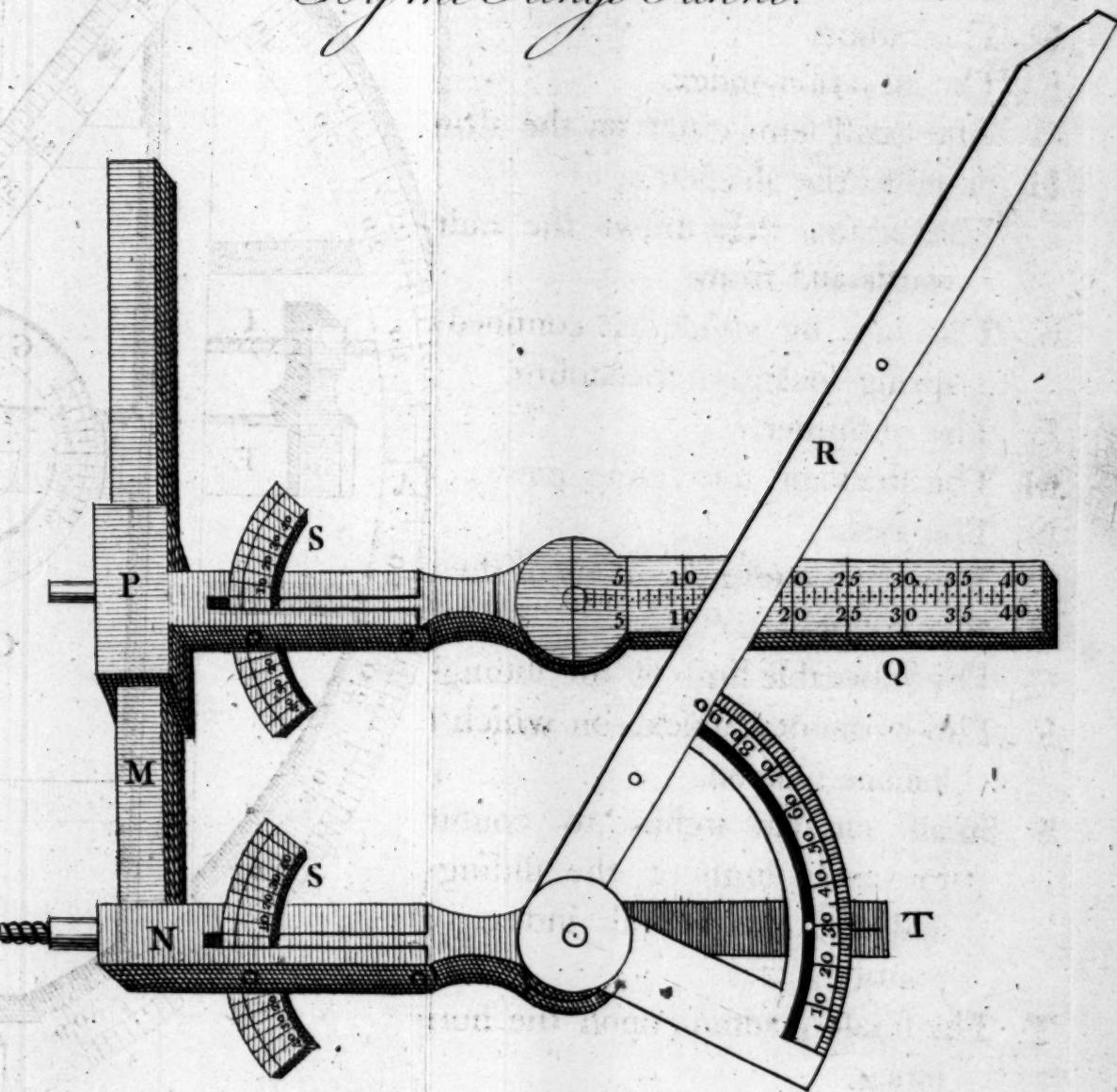
- A** The semi-circle.
- B** The diameter.
- C** The altimeter.
- D** The chord.
- E** The radius.
- F** The elevation-index.
- G** The small semi-circle on the altimeter.
- H** Stays to the altimeter.
- I** The screw, that draws the radius towards and from
- K** The stay, by which it is confined to the spring-socket or theodolite.
- L** The plummet.
- M** The stock of the sliding-piece.
- N** The axis.
- O** The key to move the screw of the radius.
- P** The sliding-piece.
- Q** The moveable limb of the sliding-piece.
- R** The horizontal index, on which the telescope is fixed.
- S** Small circular arches to confine the moveable limb of the sliding-piece, and the horizontal index, in any position, &c.
- T** The small quadrant upon the horizontal index.

FORM



To face Page 16.

DUNCOMBE & WHITTELL'S
New-invented Instrument for Measuring
STANDING TIMBER
&c
By the King's Patent.



T

M
N

A

B

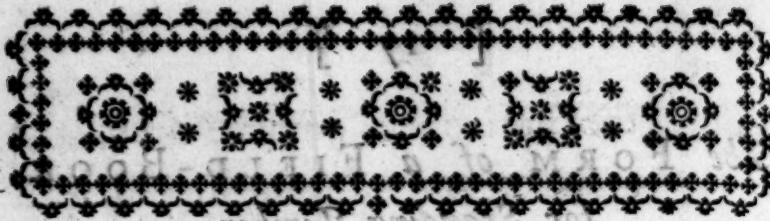
C

*The FORM of a FIELD-BOOK
for Standing Timber.*

Mark and Number.	Height.		Diam.		True Solidity.			Common Solidity.		
	F.	I.	F.	I.	T.	F.	I.	T.	F.	I.
A — 1	30	0	4	0	7	1	0	5	2	0
2	—	—	—	—	—	—	—	—	—	—
3	—	—	—	—	—	—	—	—	—	—
&c.	—	—	—	—	—	—	—	—	—	—
B — 1	—	—	—	—	—	—	—	—	—	—
2	—	—	—	—	—	—	—	—	—	—
3	—	—	—	—	—	—	—	—	—	—
&c.	—	—	—	—	—	—	—	—	—	—
C — 1	—	—	—	—	—	—	—	—	—	—
2	—	—	—	—	—	—	—	—	—	—
3	—	—	—	—	—	—	—	—	—	—
&c.	—	—	—	—	—	—	—	—	—	—

C

DIRECTIONS



DIRECTIONS

For the Use of the
INSTRUMENT.



CHAP. I.

To measure a tree in any position on level ground.

LACE the instrument at any convenient distance from the tree; then, by means of the plummet, set it in a perpendicular position; which done, screw it fast upon the staff. Set the *altimeter* in the exact position of the tree *, and screw it fast. With your tape-line

* That is, if the tree recline or incline, so much must the *altimeter* recline or incline; or, if the tree be perpendicular, the *altimeter* must also be perpendicular.

measure

DIRECTIONS

Measure the horizontal distance from the tree to the *axis* of the instrument, and with your *key** move the *radius*, until that distance be cut upon it by the inside of the *diameter*. Thus is your instrument properly rectified †.

To take the length of a tree.

Put your left hand upon the end of the *elevation-index*, and your right upon the shank of the sliding-piece close to the *stock*, on the under side; then move the *index* downwards, until you see, through the sights, the bottom of the tree cut by the *horizontal wires*; and there note the feet and inches marked by the *index* upon the *altimeter* below the point of sight or horizontal line. Move the *index* upwards, until you see the part || to which you would measure, cut likewise by the *horizontal wires*; and there note also the feet and inches marked by the *index* upon the *alti-*

* In the form of a watch-key for that purpose.

† The instrument is to be rectified thus in all cases.

|| As far as the timber extends.

meter, above the point of sight: these two quantities added together, give the exact length of the tree; which insert in the second column of your field-book, and then proceed

To take the girth.

With your tape-line measure the circumference of the tree in that part whence you took your horizontal distance; and let the distance on the *radius*, which was before cut by the inside of the *diameter*, be now increased by one sixth of the above-mentioned circumference ||: this done, lower the *elevation-index* to the part of the tree, where you purpose to take the diameter; and screw it fast. Set the moveable limb of the *sliding-piece* quite straight, and the edge of the *horizontal index* upon the first division thereof. Turn the whole instrument about to the left hand, until you see, through the sights, the left side of the tree

|| As the tape-line cannot be applied to the center of the body of the tree; and as the distance of that point to the circumference is nearly one sixth part thereof, the above allowance becomes necessary.

cut

cut exactly by the *perpendicular wires*: then (the *instrument* being fixed) move the sights only upon the *sliding-piece*, until you see the right side of the tree cut also by the *perpendicular wires*; and you will find the true diameter marked by the *horizontal index* upon the *sliding-piece*. Having entered this in the third column of your field-book, you may proceed

To measure the boughs.

As the *radius* was increased by a sixth, part of the circumference to take the diameter, it must now be reduced to its former quantity, *viz.* the distance from the tree to the *axis* of the instrument. This done, move the *elevation-index* upwards, until the bough becomes visible through the sights, and there screw it fast. Set the moveable part of the *sliding-piece* in a position parallel to the bough, with the edge of the *horizontal index* placed upon the first division thereof. Turn the whole instrument about, until you see, thro' the sights, the shoot of the bough, close to the

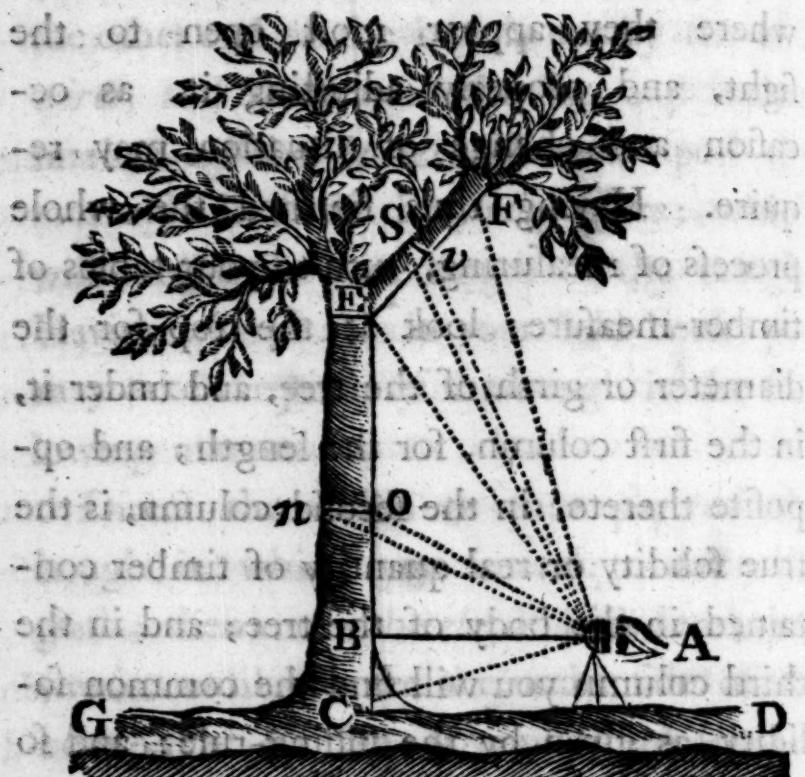
trunk of the tree, cut by the *perpendicular wires*; then move the sights, until you see the other end of the bough cut by the said wires, and there note the feet and inches marked by the *horizontal index* upon the moveable limb of the *sliding-piece*; which will exhibit the true length of the bough. Having entered this in your field-book, you may take the girth of the bough in the following manner.

Direct the sights to that part of the bough in which you intend to take the girth; then move the *elevation-index* downwards, until you see the under side of the bough cut by the *horizontal wires*; and there note the feet and inches marked by the said *index* upon the *altimeter*; this done, move the *elevation-index* upwards, until you see the upper side of the bough cut by the *horizontal wires*; and there also note the feet and inches marked upon the *altimeter* as before; subtract the former quantity from the latter, and the remainder will be the true diameter of the bough; which enter in your field-book. In like man-

ner

ner the rest of the boughs are to be measured, observing to place the instrument where they appear most open to the sight, and properly adjusting it, as occasion and change of situation may require. Having thus finished the whole process of measuring, turn to your tables of timber-measure: look at the top for the diameter or girth of the tree, and under it, in the first column, for the length; and opposite thereto, in the second column, is the true solidity or real quantity of timber contained in the body of the tree; and in the third column you will find the common solidity, as given by the sliding-rule: and so likewise of the boughs; all which may be transferred into your field-book at leisure.

EXAMPLE I.



Let EBC represent a tree standing upon the level ground GD. Place your instrument in a perpendicular position by the *plummet* at any convenient distance, as at A. Set the *altimeter* in the exact position of the tree. With your *tape-line* measure the distance from the tree to the center of the instrument, *viz.* BA (which we will suppose to be 17 feet). Move the *radius* either

either backwards or forwards, as there may be occasion, until that number of feet be cut upon it by the inside of the *diameter*. Then direct the sights to C by depressing the *elevation-index*, and there note the number cut by it upon the *altimeter* downwards from the center (suppose five feet); this done, elevate the sights to the direction AE, and there also note the number cut upon the *altimeter* by the *elevation-index*, from the center upwards, which we here suppose 25 feet: add these two numbers together, and their sum (30 feet) will be the whole length of the tree; which enter in the second column of your field-book.

Next, with your *tape-line* measure the circumference or girth of the tree, in the place B whence you took your distance, and increase the number on the *radius* by one sixth of that circumference: then depress the *elevation-index* to that part of the tree where you design to take the diameter, as at no, and screw it fast: lay the moveable limb of the *sliding-piece* quite straight, and the

horizontal

horizontal index upon the first division thereof; turn the whole instrument to the left, until, through the sights, you see that side of the tree cut by the *perpendicular wires*: then move the sights, until you see the other side of the tree cut in like manner by the *wires*; note the number cut by the *horizontal index* upon the moveable limb of the *sliding-piece*, and you will find the true diameter of the tree ~~now~~, marked thereon, (suppose four feet,) which enter in the third column of your *field-book*.

The girth being thus obtained, move the *radius* back to the former distance, *viz.* 17 feet: then raise the *elevation-index* to the direction of the bough EF, which you design to measure, and there screw it fast: set the moveable limb of the *sliding-piece* in a parallel position to the bough, and lay the *horizontal index* upon the first division thereof. Now turn the whole instrument about, until, through the sights, you observe the shoot of the bough at E, cut by the *perpendicular wires*: then move the sights until you see the extremity

tremity of the bough, at F, cut also by the perpendicular wires; and there note the number marked by the *horizontal index* upon the moveable limb of the *sliding-piece*, which determines the true length of the bough: this done, direct the sights to that part, as S v, of the bough where you intend to measure the diameter; depress the *elevation-index*, until, through the sights, you observe that point v in the under side of the bough which is cut by the *horizontal wires*; and there note the number marked upon the *altimeter* by the *elevation-index*; then raise the said *index*, until, through the sights, you see the upper side of the bough, at S, cut by the *horizontal wires*; there also note the number marked upon the *altimeter*: subtract the former number from the latter, and the remainder will be the diameter of the bough: then refer to your tables, as before-mentioned, for the solid content.

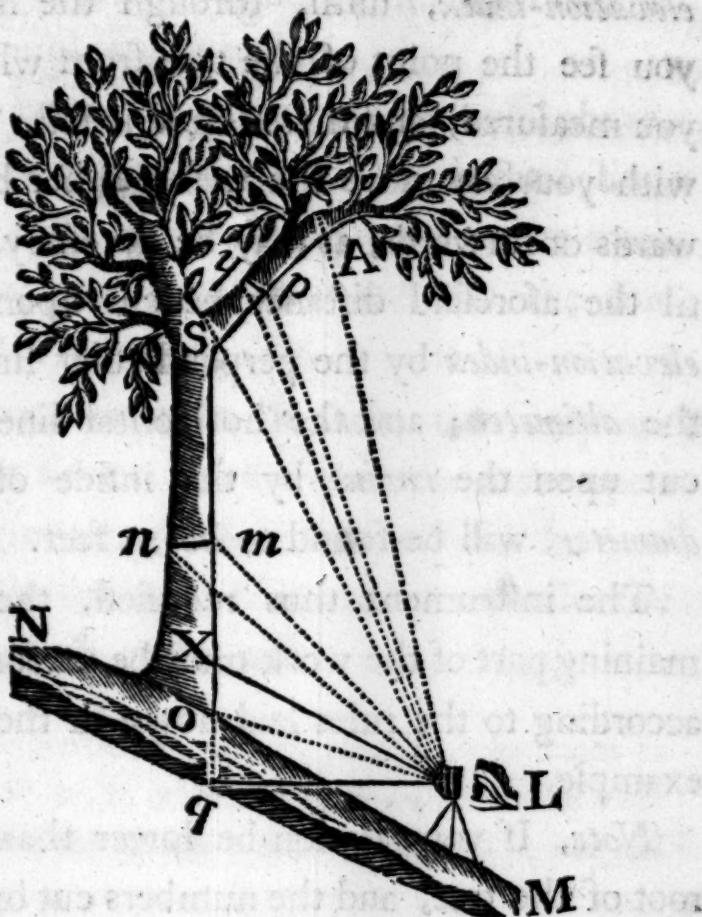
With regard to the use of this instrument, it being necessary in all cases to adjust it according to the directions at the beginning of this chapter, and the whole future

ture process being nearly the same with the foregoing; we shall proceed to give such examples, as may serve to obviate whatever difficulties are likely to occur, in finding the length of trees situated on slanting ground, crooked trees, &c. and likewise where they are inaccessible by the intervention of a river, or other obstacle.

C H A P. II.

To measure a tree in any position on slanting ground.

E X A M P L E II.



L E T O X S represent a tree standing upon the slanting base N M: place your instrument at any convenient distance, as at L, and there fix it perpendicular to the horizon;

horizon; set the *altimeter* in the exact position of the tree, and screw it fast. This done, measure the distance, $X L$, from the tree to the instrument with your *tape-line*, which we here suppose 24 feet: move the *elevation-index*, until, through the sights, you see the point of the tree from whence you measured, and there screw it fast: then with your *key* move the *radius* either backwards or forwards, as may be necessary, until the aforesaid distance be cut upon the *elevation-index* by the perpendicular line of the *altimeter*; and the horizontal line $L q$, cut upon the *radius* by the inside of the *diameter*, will be found to be 19 feet.

The instrument thus rectified, the remaining part of the work must be performed according to the rules laid down in the first example.

Note, If your station be lower than the root of the tree, and the numbers cut by the *elevation-index* upon the *altimeter* be, at the same time, above the horizon*, their difference

* By the horizon is meant that imaginary line, which passes through the sights when the instrument stands

difference gives the true length of the tree. On the contrary, if your station be higher than the top of the tree, and the numbers cut by the *elevation-index* upon the *altimeter* be *below the horizon*, the length of the tree will be equal to the difference of those numbers, as before.

Moreover, if one number be found above, and the other below the horizontal line, drawn from the point of station to the tree; in this case their sum exhibits the true length of the tree.

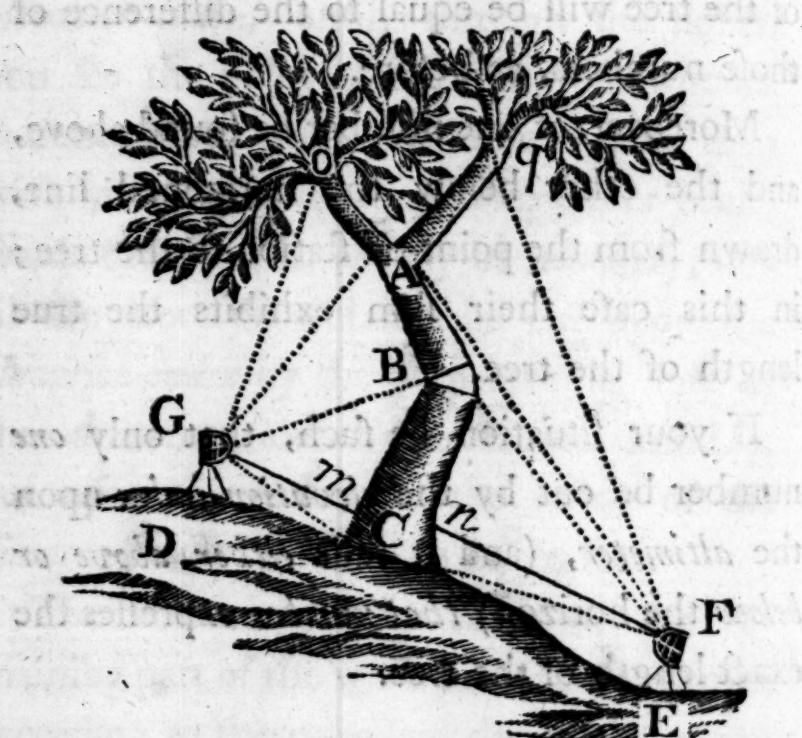
If your situation be such, that only *one* number be cut by the *elevation-index* upon the *altimeter*, (and it falls either *above or below the horizon*) that number expresses the exact length of the tree.

stands perpendicular, and the *elevation-index* points to *no degrees*: or, in other words, when it cuts the *center division* on the *altimeter*, and lies parallel to the *real horizon*.

C H A P. III.

To measure an irregular tree, situated upon ascending or descending ground.

E X A M P L E III.



LE T ABC represent a tree standing upon the slanting base DE: fix your instrument perpendicular to the horizon at a convenient distance FC, or GC, and set the *altimeter* in the exact position of the lower part (BC) of the tree; then with your tape-line measure the distance nF, or

or mG , and proceed according to the rules laid down in the second chapter.

This done, and the measurement of the lower part of the tree obtained, raise the *elevation-index*, until you see the point B * ; screw it fast, and observe the number cut upon the said *index* by the perpendicular line of the *altimeter*. Set the *altimeter* in the exact position of the upper part (A B) of the tree; screw it fast. Move the *radius* backwards or forwards, as occasion may require, until the number before observed on the *elevation-index*, be again cut by the perpendicular line of the *altimeter*. Thus is your instrument rectified for the second operation, which must be performed as follows.

Observe the number cut upon the *altimeter* by the *elevation-index*, when the sights are directed to B; and also the number cut upon the *altimeter* by the said *index*, when they are directed to A: the former of these numbers subtracted from

* The height to which you have already measured.

the latter, gives the length, A B, of the upper part of the tree. The diameter, and likewise the boughs, must be measured as before directed in the first example *.

C H A P.

* It must here be observed, that there will be a small error in this measurement, from the circumstance of the crooked part at B: for, if you measure on the exterior side of the crook (from F), then is the length, already taken, more than the *mean length*, by half the tangent of the angle of the tree's reclin-
ation from a right line. On the other hand, if you measure on the interior side of the crook (from G), then the length, already taken, will be less than the *mean length*, by half the tangent aforesaid. Now this error, though very trifling, may be corrected, and the true measurement taken in the following manner;

- viz.*
1. Measure the length of the tree, as before directed, both on the exterior and interior sides of the crook; add them together, divide the sum by two, and the quotient will be the *mean length* required. Or,
 2. When the *altimeter* is set in the position of the second part of the tree (A B), observe the angle of the tree's reclin-
ation or inclination upon the *small semi-circle* of the *altimeter*, and also measure the diameter of the tree in the crooked part. This done, set the *altimeter* in a perpendicular position, and the *elevation-index* to the angle of the tree's reclin-
ation, or inclina-

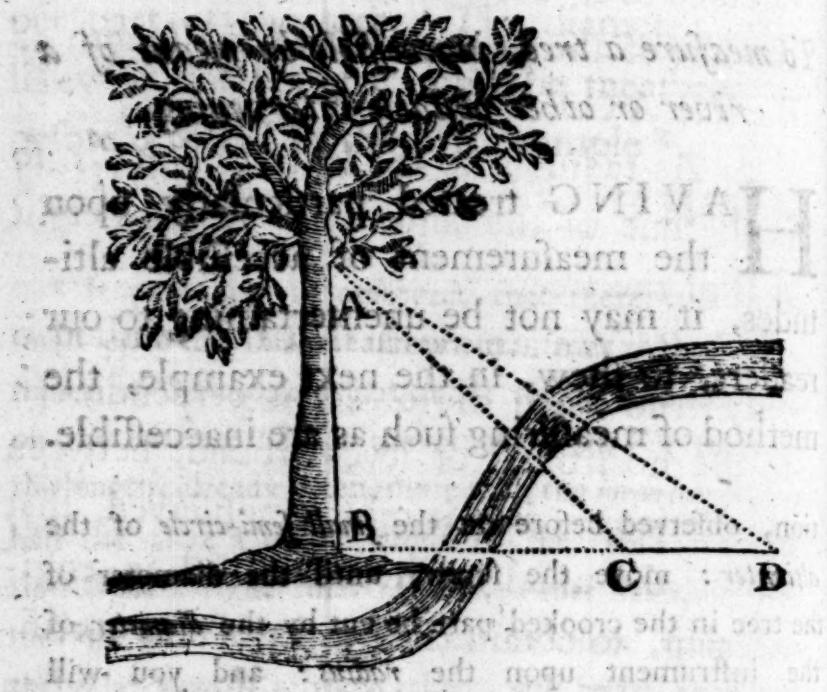
C H A P. IV.

To measure a tree, inaccessible by means of a river or other obstacle intervening.

HAVING treated particularly upon the measurement of accessible altitudes, it may not be unentertaining to our readers, to shew, in the next example, the method of measuring such as are inaccessible.

tion, observed before on the *small semi-circle* of the *altimeter*: move the screw, until the diameter of the tree in the crooked part be cut by the *diameter* of the instrument upon the *radius*: and you will find the *tangent* of the angle of the tree's reclinature or inclination cut by the *elevation-index* upon the *altimeter*. Add half this tangent to the length of the tree, if on the interior side of the crook, and the sum will be the *mean length* required. On the contrary, if on the exterior side of the crook, subtract half this tangent from the length of the tree, and the difference will be the *mean length* required.

EXAMPLE IV.



Let $A B$ represent a tree, rendered inaccessible by the intervention of a river. Place your instrument at any convenient point, as at D , and take the angle $B D A$: enter it in your field-book. Advance to C , and there take the angle $B C A$; which also insert in your field-book: measure the distance $C D$; and insert it in your book: subtract the angle of altitude observed at D , from the angle at C , and the remainder will be the angle $C A D$: then the proportion will be,

I. As

1. As the sine of the angle at A is to the distance C D between your stations; so is the sine of the angle at D to the length of the line A C.

2. As radius is to the length of A C; so is the sine of the angle at C to the height A B of the tree.

N. B. We are aware that this method is only true when the object is perpendicular to the horizontal or level ground, between the stations. But it must be observed, that this is the usual method practised in engineering, to obtain the height of any fortification. To obviate every difficulty, when the ground between the stations is irregular, the inventor of this has constructed another instrument for the use of His Majesty's engineers, which will readily determine, *without calculation*, the true height and distance of any tower or battery, or of any part thereof; and also its projection or depression, either above or below the horizon.

C H A P. V.

Of land-surveying, &c.

HAVING already * mentioned the difficulties attending the surveying of hilly, or uneven ground, with the *theodolite*; and remarked that, amidst such a variety of calculations, surveyors may be liable to dangerous errors; we shall further beg leave to observe, that notwithstanding Mr. HUME § (editor of *Wilson's Surveying*) seems to reject the use of the *theodolite*, and other graduated instruments; yet we can by no means agree with that gentleman, in recommending the use of the *chain alone*, as fully sufficient in *all* cases. On the contrary, we positively affirm, that no estate or lordship can be correctly surveyed by the *chain alone*, unless the land be *truly level*. For in measuring over ascents and descents, it is evident, the measurement of such line will be much longer than the horizontal or base line; and,

* In the Introduction.

§ In his Argument, p. 291.

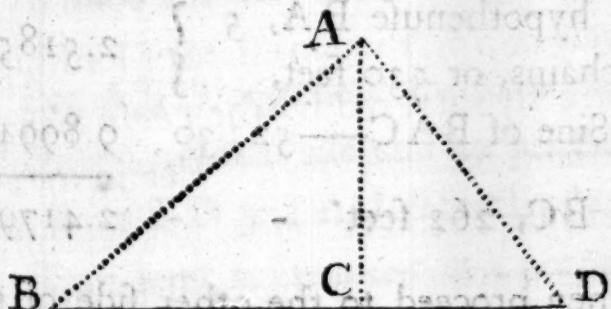
consequently,

consequently, no *true* plan can be formed, without the assistance of some graduated instrument, to take the angles of acclivity or declivity, previous to calculation.

We shall now proceed to illustrate by comparison, in the following chapter, the advantage of this our instrument over the *theodolite*, &c. in the practice of surveying, particularly of hilly ground.

C H A P. VI.

The process of surveying hilly ground with the theodolite, &c. from WILSON's Surveying, Sect. I. p. 146.



" **L**E T the mountain **BAD**, be supposed to stand upon the horizontal line, or plane **BCD**, and its perpendicular altitude **AC**, and the whole horizontal line of the plane **BD** is required.

" Bring the instrument to the bottom of
 " the mountain or hill at B, and let your
 " assistant go to the top of the hill at A,
 " and place a mark that may be seen from
 " B, and elevate your instrument, so that
 " you can, through the sights, see the mark
 " at A, and observe the degree of altitude,
 " which suppose 37 deg. 30 min.

" The angle ABC, found as above, being
 " 37 deg. 30 min. the angle BAC is 52
 " deg. 30 min. (by Theor. V. the angle
 " BCA being a right-angle;) therefore to
 " find the base BC, by *case the first of right-*
angled plane triangles,

" As radius	-	-	-	10.00000
" To hypotenuse BA, 5				2.51851
" chains, or 330 feet,				
" So Sine of BAC — 52 : 30				9.89946
" To BC, 262 feet	-	-	-	2.41797

" Then proceed to the other side of the
 " mountain or hill at D, and with your in-
 " strument take the angle CDA, as before,
 " which suppose 56 deg. 00 min, and let the
 " side DA, when measured, be 270 feet,
 " from thence find the base CD, as before,

gaind "

" The

" The angle D being 56° 00', the angle
" DAC will be 34° 00' to find CD.

" As radius 10.00000

" To AD — 270 feet — 2.43136

" So sine of DAC 34° 00' — 9.74756

" To CD — 151 feet — 2.17892

" The Line BC — 262 feet.

" Added to CD — 151 feet.

" The sum is the whole line BD 413 feet.

N. B. Mr. WILSON has omitted the calculations for the perpendicular height.

*The process of surveying the same hilly ground
with the new-invented instrument.*

Let ABD represent the same mountain as before, whose base and perpendicular are the lines BD and AC respectively.

Place your instrument in a perpendicular position at B, and at A set up a mark, of equal height with your instrument. Raise the elevation-index, until you see the mark at A through the sights, and there screw it fast:

fast: then with your chain measure BA, the side of the hill, (which admit to be 20 poles, or 330 feet, agreeable to Mr. Wilson's example.) This done, set the *altimeter* perpendicular to the horizon, and screw it fast. Move the *radius*, either backwards or forwards, as occasion may require, until the number above-mentioned be cut upon the *elevation-index* by the perpendicular line of the *altimeter*; and you will find the segment BC, of the base-line BD, to be 15 poles and 22 links, or 262 feet, cut by the inside of the *diameter* upon the *radius*; likewise the perpendicular height AC to be 12 poles 4 links, or 200 feet 7 inches, cut by the *elevation-index* upon the *altimeter*. Now remove your instrument to the top of the hill at A, and direct the *elevation-index* downwards, until, thro' the sights, you see the mark at D; having screwed it fast, measure AD with your chain (which suppose to be 16 poles 4 links, or 270 feet). Then proceed as on the other side of the hill, and you will find the segment CD, of the base BD, to be 9 poles 4 links,

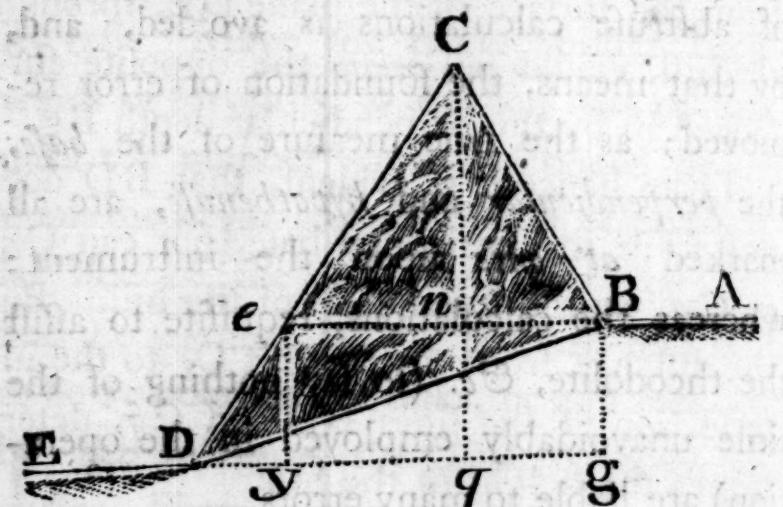
4 links, or 151 feet, The sum of these segments of the base gives 25 poles 1 link, or 413 feet, for BD, the base-line required.

From hence it is manifest, that a series of abstruse calculations is avoided, and, by that means, the foundation of error removed; as the true measure of the *base*, the *perpendicular* and *hypotenuse*, are all marked *at once* upon the instrument: whereas the calculations, requisite to assist the theodolite, &c. (to say nothing of the time unavoidably employed in the operation) are liable to many errors.

Thus having, we apprehend, clearly demonstrated, by this comparative view, the advantage of our instrument over the theodolite, &c. both with regard to ease and expedition; we shall farther illustrate its use in measuring hills situated upon inclined bases.

C H A P. VII.

*Concerning the measurement of a mountain, or
hill, when the ground on each side thereof
is not in the same horizontal plane.*



LET AB and DE represent the plane surface on the opposite sides of the hill BCD: then will BD form the oblique, and Dg the true horizontal base. Now take an observation at B, Cn will be the perpendicular height, and Bn the segment of the horizontal base. On the contrary, Cq will be the perpendicular height, and Dq the other segment of the base, if the observation be made at D. We may here observe, that if a level from the plane surface

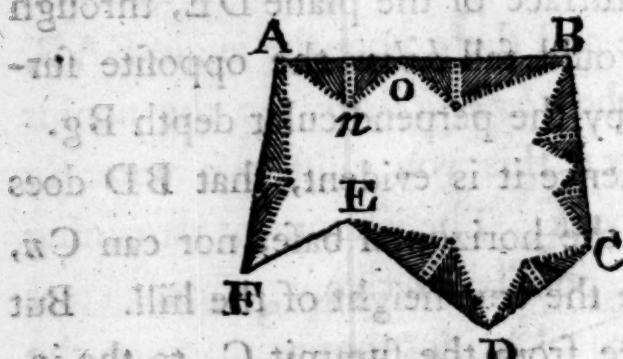
face A B was continued through the hill, such level would appear *above* the opposite surface D E, by the perpendicular height e y. On the other hand, a level carried from the surface of the plane D E, through the hill, would fall *below* the opposite surface A B, by the perpendicular depth B g.

From hence it is evident, that BD does not form the horizontal base, nor can C n, or C q, be the true height of the hill. But the distance from the summit C, to the intersection of the lines BD and C q, determines the height of the hill.

Note. As the horizontal base D g, is to the difference B g of the heights q C, n C, so is the segment D q to a fourth number, which taken from the perpendicular C q, leaves the height required.

C H A P. VIII.

To measure the ground-plat of an irregular field, &c.



LET ABCDEF be the boundary of an irregular field; the dotted lines representing the rise and fall of the ground. First, cause large and conspicuous marks to be erected in all the angles of the field, at an equal distance from the hedge, making your observations without the field.

This done, remove the mark from A. Fix your instrument in a perpendicular position, in the same place where the mark stood. Set the index of the *theodolite-part* upon the 360th degree. Turn the whole about, until, through the sights,

you

you see the mark at F, and there screw it fast. Observe the bearing of the compass*; which must be entered in your field-book.

Next move the index of the *theodolite-part*, until, through the sights, you see the mark at B, and there note the angle F A B, cut upon the *theodolite-part* by the nonius of its index; this you must also enter in your field-book. The instrument remaining in the same position, let your assistant erect a mark of equal height therewith, upon the summit of the first rise of the ground at n. Raise the *elevation-index*, until, through the sights, you see the mark at n, and there screw it fast. Measure the distance A n, and proceed to find the segment of the base, &c. as directed in Chap. VI. This done, remove your instrument to n. Place a mark at o, and depress the *elevation-index*, until, through the sights, you perceive the mark at o. Screw it fast. Then measure the distance n o, and proceed to

* The degrees, &c. to which the needle points; it being the angle that the line A F makes with the meridian.

find

find the segment, as before directed. Continue the process in the same manner to B. Add the several segments together, and the sum will be the true length of the base-line AB; which enter in your field-book. Move the mark from B, and fix your instrument where the mark stood. Let the mark be replaced at A; then set the index of the theodolite-part to the 360th degree. Move the whole about, until, through the sights, you see the mark at A, and there screw it fast. Move the index of the theodolite-part, until, through the sights, you see the mark at C; there note the angle ABC, and measure the distance BC, as before directed. Proceed in this manner to measure the remaining sides and angles of the figure, and insert them in your field-book.

It may be here necessary to observe, that the marks erected in the several angles of the field must be upright, and the instrument, upon each removal, placed on the spot where the mark stood; for without this precaution an error will arise.

N. B.

N. B. To prove the truth of your mensuration, multiply the number of sides enclosing the field by 2; subtract 4 from the product, and the remainder, multiplied by 90, will be equal to the sum of the supplements of all the external angles taken in measuring round the field. If the internal angles had been measured, the above rule would have given the sum of those angles themselves.

The TOWN FIELD or COMMON.

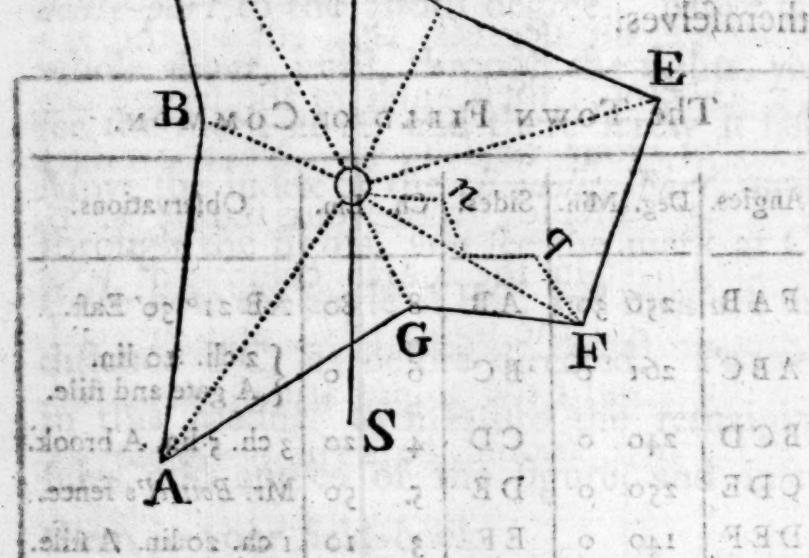
Angles.	Deg. Min.	Sides.	Ch.	Lin.	Observations.
FAB	256 30	AB	8	80	AB 21° 30' East.
ABC	261 0	BC	6	0	{ 2 ch. 10 lin. { A gate and stile.
BCD	240 0	CD	4	20	3 ch. 5 lin. A brook.
CDE	250 0	DE	5	50	Mr. Bottrel's fence.
DEF	140 0	EF	3	10	1 ch. 20 lin. A stile.
EFA	292 30	FA	6	30	Mr. Jones's fence.

CHAP. IX.

To measure a field at one station, and to pro-

vide a plan tract the same.

Theodolite
Field
Survey
and
Tract
the
same
at
one
station
and
to
pro-
vide
a
plan
tract
the
same.



LET ABCDEFGA represent an irregular field. Fix your instrument vertically in some convenient part thereof, as at O, from whence the angular points of the field are visible. Set the *index* of the theodolite-part to the 360th degree. Turn the whole about, until the needle points directly

rectly to the north and south of the compass *, and there screw it fast. Then direct the sights to A. Note the degrees, &c. cut upon the theodolite-part by the nonius; and enter them in the second column of your field-book. This done, measure O A, the distance from your station to A; insert it in the fourth column of your book. Then direct the sights to B, observing the degrees, &c. cut by the nonius as before: these enter in the second column of your field-book. Next measure O B, the distance from your station to B, which insert in the fourth column of your book. Point the sights to C, and proceed, as before, until the angles are all measured. But if there should be a rise or fall in the land, from your station to any of the angles, as in the line O n q F, then must the base or horizontal line be found, as directed in Chap. VIII.

* The sights will then form the meridian line N S.

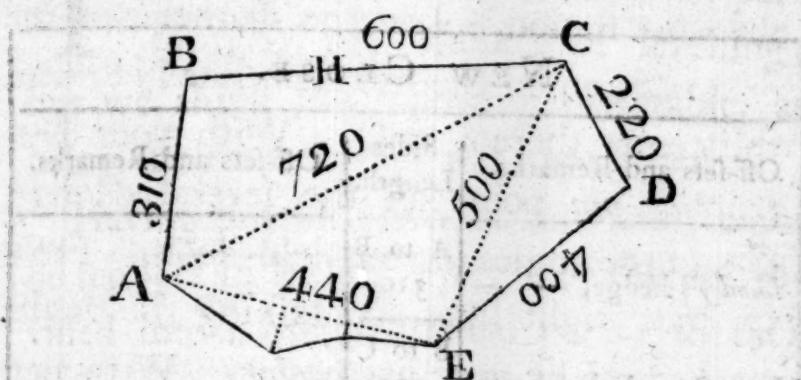
*Directions for protracting * the former field.*

With your pencil draw the meridian line N S, and assume any point, as O, therein for your station. Lay the diameter of the protractor upon the meridian line N S, with the center thereof at O. With your protracting-pin point off the several degrees, &c. of the angles in your field-book. From O draw right lines, containing the angles marked off by your protractor. With your compasses, from a scale of equal parts, set off (from your field-book) the distances O A, O B, &c. measured from your station O. Join the several points, thus determined, until the whole be enclosed, and you will have the true representation of the field.

* We would recommend the use of an entire circle for protracting with.

C H A P. X.

To measure an irregular-sided field with the chain alone.



LET ABCDEA represent a level but irregular-sided field. Erect visible marks in all the angular points, A,B,C,D,E. This done, run your chain from A in a direct line to B, also from B to C, and insert their measure in the middle column of your field-book. From C, run your chain directly to your first station A, and enter its measure in the field-book: thus will the triangle ABC be compleated. Proceed again from A, and measure in a straight line to E, for the crooked hedge AE: take off-sets from the hedge in the several crooks as you go along, and insert them in your field-book, according to the form annexed.

nected. Then measure from E to C, from C to D; and lastly from D to E: thus will the proper requisites for protracting the field be obtained.

NEW CLOSE.		
Off-sets and Remarks.	Sides Length.	Off-sets and Remarks.
<i>Lumley's hedge, — —</i>	A to B 310	
<i>Into Crump's lane gate,</i>	B to C 200 600	
<i>Diagonal, — — —</i>	C to A 720	
	A to E 000 200 300 440	000. <i>Lloyd's hedge,</i> 070. 020. 000.
<i>Diagonal, — — —</i>	E to C 500	
<i>Kerry's lane, — — —</i>	C to D 220	
	D to E 400	

C H A P. XI.

Of the use of the instrument in levelling.

TH E R E are various methods for performing the business of levelling; but we think the following preferable, as being the most certain and expeditious.

Having provided two station-staves, eight or ten feet in length, every foot thereof divided into a hundred equal parts; to each staff must be fitted a vane*, about three inches square, to slide with a screw, in the back part, by which it may be confined at any height upon the staff.

D I R E C T I O N S.

Place your instrument in a right line, joining the two stations to be levelled, and fix it perpendicular to the horizon. Set the elevation-index to the center-division of the semi-circle, and there screw it fast. The instrument thus rectified, look through the sights, and cause one of your assistants (pro-

* The face of the vane should be painted white, and a black line drawn horizontally across the middle.

vided for that purpose) to slide the vane upon the staff, until the black line thereon be cut by the horizontal wires, noting the divisions upon the staff from the ground to the said black line. Then remove to the other side of your instrument, and look through the sights, causing your *other* assistant, at the same time, to move the vane upon the *other* staff, until the black line and the horizontal wires coincide. Note the divisions upon the staff, from the ground to the said black line. In consequence of these observations, if the ground be level, the number of the divisions cut by the vanes on both staves will be equal. On the other hand, if those numbers cut by the vanes be unequal, their difference will shew how much the ground declines from a true level.

Where Obstacles intervene.

If the places to be levelled have intervening obstacles, or should be too far distant from each other for one observation,

you

you must take as few stations * as possible, and keep a regular account of the numbers cut upon the staves: let those of the back station be put in the first column, and those of the fore station in the third, observing to register the number of stations in the intermediate column. As for example:

Back Stations.	Stations.	Forward Stations.
0 29	1 H A H D	32
1 78	2	2 01
1 99	3	2 95
2 21	4	2 56
6 27		8 84
		6 27
		Declivity 2 57

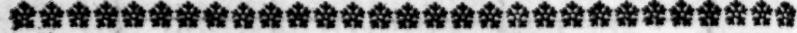
Thus you may determine not only the acclivity or declivity of the ground at every *separate* station, but also of *the whole* together. For the difference between the

* The forward staff will become the backward staff at every new observation.

respective

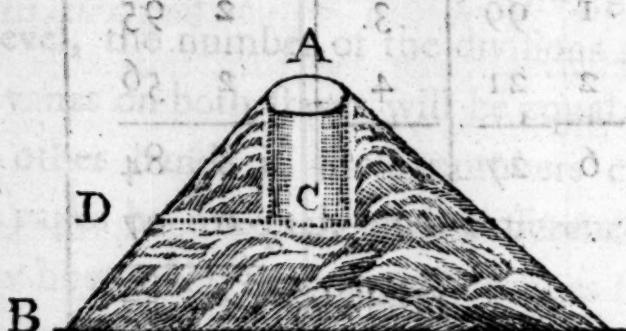
respective sum of the forward and the backward stations gives the ascent or descent required.

Note, In levelling rivers, the first and last station must be taken close to the water's edge. But the intermediate stations may be taken, at pleasure, in the meadows or fields adjoining.



CHAP. XII.

Of the use of the instrument in mineing.



To find the horizontal point for opening a drain.

FIX your instrument in a perpendicular position at A, the head of the shaft of the mine; erect a mark of the same height therewith at the foot of the hill B. Depress the *elevation-index*, until,

til, thro' the sights, you see the mark at B, and there screw it fast. Then the depth of the shaft AC being known, and the *altimeter* fixed perpendicular to the horizon, move the *radius* as occasion requires, until the aforesaid depth AC, be cut upon the *altimeter* by the *elevation-index*. This done, you will find the true length of the drain from the bottom of the shaft C to D, cut by the inside of the *diameter* on the *radius*, and also the distance from the shaft-head A, to the part D on the side of the hill, where the drain must be opened, cut upon the *elevation-index* by the perpendicular line of the *altimeter*.

C H A P XIII.

A certain method of finding which way the LOAD of a mine inclines, in order to sink a new shaft.

B EING provided with two station-staves, about four feet high, with a socket in the top wherein a candle may

may be fixed; place your instrument directly in the center of the shaft, and one of the staves, with a lighted candle therein, in the first angle or turning of the drift, at equal distance, as near as possible, from the sides of the mine. Then lay the *index* of the *theodolite-part* to the 360th degree: turn the whole about, until the needle hangs directly over the north and south points of the compass, and there screw it fast. This done, move the *index* of the *theodolite-part*, until, through the sights, you see the lighted candle, and then observe the degrees, &c. cut upon the *theodolite-part* by the *nonius* of it's *index*, which put down in the second column of your memorandum-book, according to the form annexed. With your *tape-line* measure the distance from the center of your instrument to the candle, and enter it in the third column of your book.

Now transpose both the instrument and staff, fixing the former perpendicularly on the spot where the staff was, and the latter where the instrument stood. Erect the other staff in the next angle of the drift, in the manner

manner as above directed. Lay the index of the theodolite-part as before, turning the whole about, until you see the candle at the first station; and there screw it fast. Move the index of the theodolite-part, until you see the candle in the second station; observe the degrees cut by the nonius of its index, and enter it in the second column of your book. Measure the distance from your instrument to the second candle, which enter in the third column of your book.

Now change the stations of the instrument and staves: the former must be fixed in the spot where the second candle stood, and that must be removed to the next angle of the drift, while the first must be placed where the instrument was last erected. This done, proceed as before directed, until the whole be finished. The measurement in the mine being taken, you must take the same above-ground in the following manner.

Cover the mouth of the shaft with boards, and place your instrument perpendicularly in the center thereof. Then the index of the

theodolite-part as before directed.

theodolite-part being fixed to the 360th degree, turn the whole about, until the needle stands directly over the north and south points of the compass, and there confine it. Move the index of the theodolite-part to the number of degrees, &c. of the first station taken in the mine, and entered in your memorandum-book. This done, and the instrument remaining in the same position, let your assistant erect a mark of equal height therewith, in a direct line with the sights, about a yard farther than the distance of the first measure in your book. Then raise or depress the elevation-index, until, thro' the sights, you see the said mark; and having screwed it fast, (the altimeter at the same time being confined in a perpendicular direction) move the radius until the said first measure be cut thereon by the inside of the diameter. You will then find the distance to be measured upon the surface of the land, from the instrument to the next station, cut upon the elevation-index by the perpendicular line of the altimeter, which enter in the fourth column of your

your book. You will find also the perpendicular ascent or descent of the ground in that distance, cut upon the *altimeter* by the *elevation-index*; and this must be entered, if an acclivity, in the fifth; if a declivity, in the sixth column of your book. Then with your *tape-line* measure the distance as inserted in the fourth column of your book, *viz.* from your station towards the mark. At the termination of this distance fix your instrument.

Let your assistant remove the first mark to the spot on which the instrument stood. Set the *index* of the *theodolite-part* to the 360th degree. Turn the whole about, until you see the aforesaid mark in its new station, and there screw it fast. Move the *index* of the *theodolite-part* to the number of degrees, &c. inserted in your book at the second station under ground. Cause your assistant to erect another mark, about a yard beyond the distance entered in your book at the second station, as before directed. Raise or depress the *elevation-index*, until, thro' the sights, you see the said mark; there screw it fast.

fast. Proceed now in all respects as before laid down, until the whole be accomplished.

Then the difference between the respective sums of the ascents and descents (being added to, or subtracted from, the depth of the main shaft) gives the depth of the shaft required, according as the sum of the ascents was greater or less than that of the descents: the spot, therefore, where the last measurement terminated, will be the direct place where the new shaft must be opened.

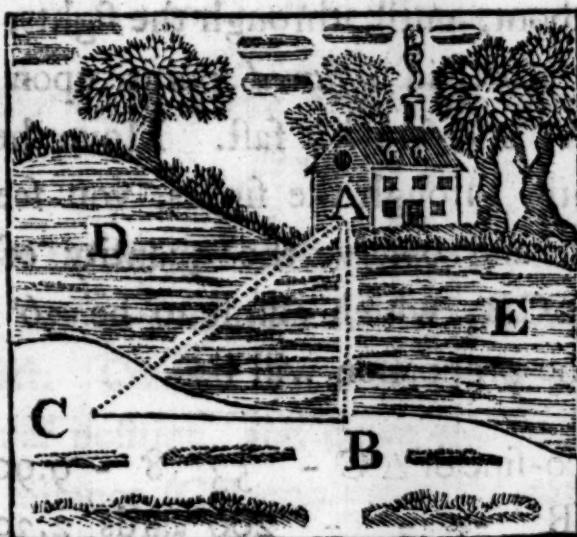
FORM of a MEMORANDUM-BOOK.

**First Station directly in the Center of the Shaft,
70 Feet deep.**

Number of Stations.	Angles at each Sta- tion.	Dist. above ground, corresponding with those in the mine.	Declivities of the Sur- face.	Depth of the Shaft at every distance.	Observations.
		Distances between the Stations measured in the Mine.			

C H A P. XIV.

HAVING already described the uses of our instrument, (with regard to the measuring of standing timber, surveying, &c.) as far as the nature of the present work would admit; yet, perhaps, it may not be improper to subjoin some entertaining examples, which may farther serve to evince its utility in performing trigonometrical operations.

To measure the breadth of a river.

Let D E represent a river, whose breadth is required. Place your instrument at any convenient

convenient point, as at B. Lay the *index* of the *theodolite-part* to the 360th degree. Turn the instrument about, until, through the sights, you see some particular *assumed* point upon the object A; and screw it fast. This done, move the *index* to the 270th degree*. Cause your assistant to erect a mark, in a right line with the sights, at any distance, as at C. Transpose both the instrument and mark. Measure the distance CB, equal to 200 yards.

Now lay the *index* of the *theodolite-part* to the 360th degree, as before. Turn the whole about, until, through the sights, you see the aforesaid *assumed* point upon the object A; and screw it fast. Move the *index*, until, through the sights, you see the mark B, and observe the quantity of the angle ACB; which admit to be $36^{\circ} 52'$. Then the proportion will be

As the co-sine of $\angle C$ -	$53^{\circ} 8'$	-	9.90311	
Is to CB	-	-	200 yards	2.30103
So is sine of $\angle C$ -	$36^{\circ} 52'$	-	9.77812	
To BA	-	-	150 yards	2.17604

* It being at right angles with the 360th degree.

Note,

Note, If, in the foregoing process, the index of the theodolite-part were laid to the 90th degree, instead of the 270th, turn the instrument about, at your station C, until you see the mark B. Then take the angle BCA, and proceed, in all other respects, as above directed.

Note also, If you cannot fix your instrument close to the river, you should measure the distance from your station B to the edge of the water; which, subtracted from the whole line BA, gives the true breadth of the river required.

To work the above proportion upon the instrument.

Set the *elevation-index* to $36^{\circ} 52'$ * upon the *semi-circle* of the instrument, and screw it fast. Confine the *altimeter* in a perpendicular position, and move the *radius* until the distance (CB 200 yards) be cut upon it by the inside of the *diameter*. Then you

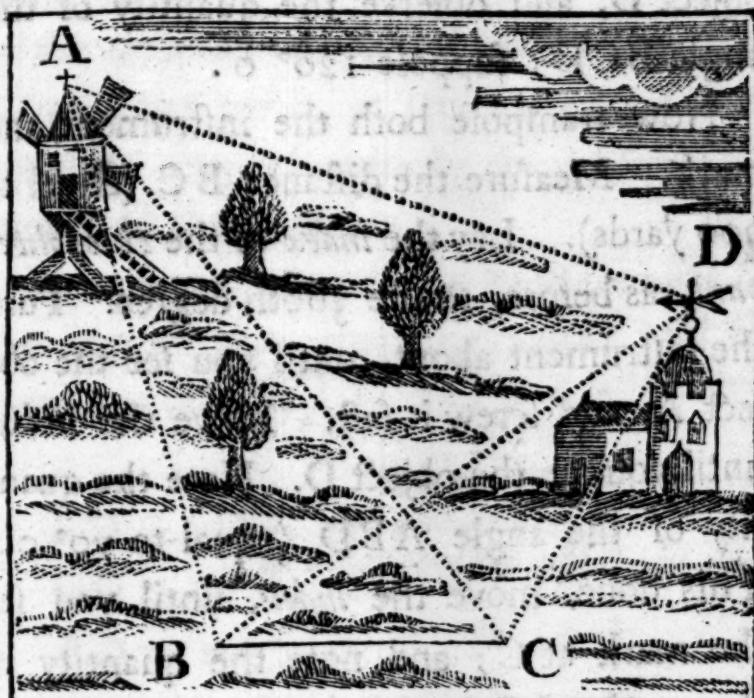
* The quantity of the angle cut by the *nonius* on the *theodolite-part*.

will find the breadth of the river (BA 150 yards) cut upon the *altimeter* by the *elevation-index*; and also the distance (CA 250 yards) cut upon the *elevation-index* by the perpendicular line of the *altimeter*.



but it is often not so. Hence we have
thus added C H A P. XV.

To measure the distance between two remote
objects.



SUPPOSE A and D to represent two remote objects, whose distance from the stations B, C, and likewise from each other, is required.

Place your instrument at C, and a mark at B. Lay the *index* of the theodolite-part to the 360th degree. Turn the instrument

about, until you see the mark at B, and screw it fast. Then move the *index*, until you see the object A. Observe the quantity of the angle BCA; which admit to be $51^{\circ} 26'$. Move the *index* until you see the object D, and observe the quantity of the angle BCD; suppose $120^{\circ} 0'$.

Now transpose both the instrument and mark. Measure the distance BC (equal to 900 yards). Lay the *index* of the theodolite-part, as before, to the 360th degree. Turn the instrument about, until you see the object A, and screw it fast. Move the *index*, until you see the object D. Note the quantity of the angle ABD (equal to $70^{\circ} 0'$.) This done, move the *index*, until you see the mark at C; and note the quantity of the angle ABC, suppose $105^{\circ} 0'$. Your observations thus compleated, proceed

To work the several proportions upon the instrument.

Set the angle ABC (105°) on the small semi-circle of the *altimeter*, to the *nonius* upon the *radius*, and screw it fast. Then set the *nonius* of the *elevation-index* to the angle

angle $B\bar{C}A$ ($51^{\circ} 26'$) upon the semi-circle of the instrument. This done, move the radius, until the distance CB (900 yards) be cut thereon by the inside of the diameter. You will then find the distance $BA = 1760$ yards, or one mile, cut upon the altimeter by the elevation-index; and also the distance $CA = 2171$ yards, or 1 m. 1 f. $34\frac{3}{4}$ p. cut upon the elevation-index by the perpendicular line of the altimeter.

By a similar process the measurement of the sides of the remaining angles will be found, as follows;

	Yards.	M.	F.	P.
$BD = 1853$,	or 1	0	$16\frac{1}{4}$.	
$CD = 1223$,	or 0	5	$22\frac{1}{4}$.	
$AD = 2073$,	or 1	1	$16\frac{1}{4}$.	

It may here be necessary to remark that, in the application of our instrument to measuring distant objects, we have been led to the following considerations.

If an angle be taken *out* of the plane of the horizon, such angle is less than the horizontal one subtending the same, or

equal, side. From an observation, therefore, taken out of the horizontal plane, no true plan can be formed, nor until it be reduced thereto; which may be effected thus.

Set the *nonius* of the *elevation-index* upon the semi-circle of the instrument, to the degrees, &c. in the angle made by the intersection of the plane of the observed angle, and the plane of the horizon. Then screw it fast. Confine the *altimeter* in a perpendicular position. Then move the *radius*, until the base-line of the observed angle be cut upon the *elevation-index* by the perpendicular line of the *altimeter*. This done, you will find the corresponding horizontal base-line cut by the inside of the *diameter* upon the *radius*.

Now set the degrees, &c. contained between the base and side subtended by the observed angle, upon the small semi-circle of the *altimeter*, to the *nonius* of the *radius*, and screw it fast. Then set the *elevation-index* to the number upon the *altimeter*, viz. the length of the side including the observed angle,

angle, upon the *altimeter*. This done, you will find the corresponding horizontal angle upon the semi-circle of the instrument cut by the *nonius* of the *elevation-index*.

Note, If the different objects form different angles of inclination to the plane of the horizon, they must be considered respectively.

It is requisite to observe, that, in very remote distances, the horizontal lines ought to be considered as tangents to an arc of the earth's circumference. To find the angle, at the earth's center, subtending the said tangent, we have the following rule:

As the semi-diameter of the earth is to the horizontal distance measured; so is the radius (90°) to the tangent of the arc required.

Now to find the length of the said arc, multiply* the earth's circumference by the quantity of the angle subtending the tangent: divide the product by 360° ; and the

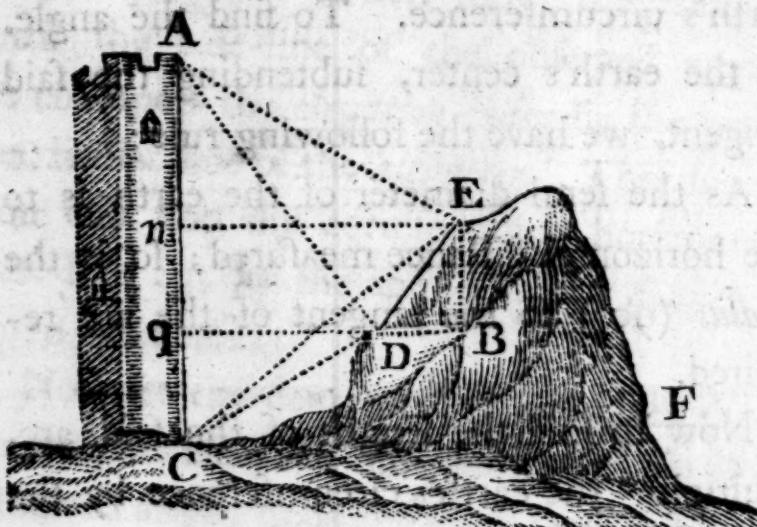
* In this operation your multiplier and divisor must always be of one and the same denomination; whether degrees, minutes, &c.

quotient

quotient will be the length of the arc; which is the true line to be delineated.

CHAP. XVI.

To find the height and distance of any tower or battery, its elevation or depression above or below the horizon, when the ground between the stations is not in the same horizontal plane.



LET AC represent a tower, and CDEF an adjacent hill. From the stations D and E it is required to determine the horizontal distances D q , E n ; the extreme distances

distances DA, DC, EA, EC; altitudes qA , nA ; and the height of the tower AC.

Place your instrument at D, and measure the angles qDC , qDA . Turn your instrument about, and measure the angle BDE. The sum of this angle, and the former qDA , being subtracted from 180° , leaves the angle ADE.

This done, transpose the instrument to E. Measure the distance DE, and take the angles of depression nEC , nED , and angle of elevation nEA . The sum of the angles nED , nEA , gives the angle DEA; to which add the angle ADE, and subtract the sum from 180° , the remainder will be the quantity of the angle DAE.

From these observations the several parts, as required in the above problem, may be found by the following calculation.

I.

As the fine of -	$\angle DAE$
Is to distance - -	DE
So is fine of -	$\angle DEA$
To the visual line -	DA

2. As

As radius - - - - $\angle qDA$

2.

Is to - - - - DA

So is fine of - - - - $\angle qDA$

To - - - - qA

And so is co-fine - - - - $\angle qDA$

To - - - - qD

3.

As co-fine - - - - $\angle qDC$

Is to - - - - qD

So is fine - - - - $\angle qDC$

To - - - - qC

And so is radius

To distance - - - - CD

4.

As radius

Is to distance - - - - DE

So is co-fine - - - - $\angle BDE$

To - - - - DB

And so is fine - - - - $\angle BDE$

To - - - - EB

5.

As co-fine - - - - $\angle nEC$

Is to - - - - nE

So is radius

To visual distance - - - - CE

Thus

Thus the distance of any proposed point of a tower, or battery, either above or below the horizon, may be found by directing the observations to that particular, proposed, point.

Note, The above proportions may be performed upon the instrument, according to the directions in the preceding chapter.

CHAP. XVII.

To measure the front of a house.

THE HEIGHT.

PLACE your instrument towards the left side of the house, at right angles with the corner. Confine the *altimeter* in a perpendicular position. Measure your distance from the house to the *axis* of the instrument. Move the *radius*, until that distance be cut thereon by the inside of the *diameter*. This done, depress the *elevation-index*, until, through the sights, you see the bottom of the house: there note the number cut upon the *altimeter* by the said *index*. Then raise the *elevation-index* until you see the top of the house, and there note the

the number cut upon the *altimeter* by the *index*: the sum of these numbers is the *height* of the house required.

THE BREADTH.

Lay the *horizontal-index* upon the first division of the moveable limb of the *sliding-piece*. Observe, through the sights, that the left edge of the front be cut by the *perpendicular wires*. Set the moveable limb of the *sliding-piece* parallel to the front. This done, move the *index* alone, until you see the edge of the house, on the right hand, cut also by the *perpendicular wires*: you will then find the required breadth expressed upon the moveable limb of the *sliding-piece* by the *horizontal-index*.

In like manner the height and breadth of a window, in the front or side of a house, may be easily obtained.

* * * To these examples already given, many others, we apprehend, will readily occur to the reader; whereby the extensive use of this instrument might be farther illustrated.

A P P E N D I X.

THE principles of geometry, confirmed by observation, shew, that angles either acute or obtuse, taken by the instrument, when *out* of the horizontal plane, are very different from their corresponding or projected angles *upon* the plane of the horizon; arising from the different situations of the observed objects: *viz.*

First, If the objects be elevated above, or depressed below, the horizon, the observed angle will be *less* than its projected angle upon the horizontal plane.

Secondly, If one of the objects be elevated or depressed, and the other *in* the plane of the horizon, the observed angle will be *greater* than its projected angle upon the horizontal plane; except the observed angle

G be

be $90^{\circ} 00'$: for, in such case, the observed and projected angles will be equal.

Thirdly, If one object be elevated and the other depressed from the horizon, the observed angle will be greater, or less, than its projected angle upon the horizontal plane, according to the difference of the angles observed upon the semi-circle of the instrument, and small circular arches.

1. If the angle, observed upon the semi-circle of the instrument, be less than the angle observed upon the small circular arches, the observed angle upon the small quadrant (fixed for that purpose upon the horizontal index) will be greater than its projected angle upon the horizontal plane.

2. If the angle, observed upon the semi-circle of the instrument, be greater than the angle observed upon the small circular arches, the observed angle upon the small quadrant will be less than its projected angle upon the horizontal plane.

N. B. If the angles observed upon the semi-circle of the instrument and small circular

cular arches be alike (or the same) the angle observed upon the small quadrant, and its projected angle upon the plane of the horizon, will also be alike, or the same.

In consequence of the addition of a *small quadrant* upon the *horizontal index*, (see Description, page 14*) it will be necessary to give a rule for resolving the following

P R O B L E M.

The measure of an angle being taken either above or below the horizon, to find the quantity of the corresponding or projected angle upon the horizontal plane.

The R U L E.

The altimeter being in a vertical position, set the nonius of the *elevation index* to the degrees, &c. contained between the plane of the observed angle and the plane of the horizon, and there screw it fast. Move the *horizontal index*, until the angle observed upon the limb of the theodolite be cut upon the *small quadrant* by its nonius.

Note the number cut upon the *moveable limb* of the sliding-piece by the *horizontal index*. This done, set the *elevation index* to 00 degrees, and screw it fast. Set the *horizontal index* to the same number (as above noted) upon the moveable limb of the sliding-piece. You will then find the corresponding angle cut by its nonius upon the *quadrant*.

To measure an angle which has different inclinations to the plane of the horizon.

R U L E.

Lay the *horizontal index* to the first division on the *moveable limb* of the sliding-piece. Turn the instrument about, until you see the object towards the left hand. Move the *horizontal index*, until you see the other object towards the right hand. Observe the number cut upon the *moveable limb* of the sliding-piece by the said *index*, and also the degrees, &c. upon the small *circular arches*.

This

This done, the observed angle may be reduced to the plane of the horizon by the following

R U L E.

Set the *elevation index* to the degrees, &c. observed upon the small *circular arches*. Note the number cut upon the *radius*. Move the *radius* until the number observed upon the *moveable limb* of the sliding-piece be cut upon the *elevation index* by the perpendicular line of the *altimeter*, and note the number then cut upon the *radius*. Now set the *elevation index* and small *circular arches* to 00 degrees, and draw the *radius* to the number first noted thereon. Lay the *horizontal index* to the same number upon the *moveable limb* of the sliding-piece as was observed the second time upon the *radius*: then will the corresponding horizontal angle be pointed out by the nonius upon the limb of the *quadrant*.

At page 18, add the following method for setting the *altimeter* in the same direction with the tree:

Before

Before the horizontal distance is measured with the tape-line, &c. take the instrument in your hand, from your station, either to the right or left side of the tree, as may be most accessible. Hold it side-ways, at any convenient distance therefrom, in a vertical position, observing to keep the diameter of the instrument always on the side next your station. Then move the *altimeter*, until you observe it form the same angle with the *radius*, as the tree forms with the horizon; or until the lines of columniation coincide.

At page 19—— When the *radius* must be moved to cut the distance measured from the tree, it is proper to observe, that if you cannot fix your station within the distance of 20 feet from the tree (it being the number of equal divisions upon the *radius*,) or if the length thereof should extend above 40 feet (the number of equal divisions upon the *altimeter*,) in such case you must move the radius to $\frac{1}{2}$, $\frac{1}{3}$, or $\frac{1}{4}$ of the distance measured. Then the height and diameter of the tree will accordingly be

be twice, thrice, or four times as much as the height and diameter measured upon the instrument. Otherwise you may call the divisions by any other denomination, as yards, poles, furlongs, miles, &c. agreeable to the denomination in which you take your distance.

To adjust the instrument.

R U L E.

The instrument being fixed upon the staff, slacken the screw, in the parallel plates, on the side elevated; at the same time straighten the opposite screw. Proceed thus until the whole instrument may be turned round upon the staff without altering the due position of the bubble in the spirit-level. In the same manner the *dendrometer* may be set vertical to the plane of the horizon by the adjusting screw, in the part by which it is fixed to the *theodolite*.

N. B. If the plane of the limb of the *theodolite* be set parallel to the plane of
the

the horizon, and the *dendrometer* set exactly vertical, so that it may be turned round without altering the true position of the plummet; it will then follow, that if the limb of the *theodolite* be exactly horizontal, the *dendrometer* will be exactly vertical.

E R R A T A.

T. F. I.

At page 17. True Solidity	7	26	$11\frac{3}{4}$
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T A B L E S.